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# Robust two-degrees-of-freedom control of hydraulic drive with remote wireless operation

Riccardo Checchin, Michael Ruderman, Roberto Oboe

Abstract—In this paper, a controller design targeting the remotely operated hydraulic drive system is presented. A two-degrees-of-freedom PID position controller is used, which is designed so that to maximize the integral action under robust constraint. A linearized model of the system plant, affected by the parameters uncertainties such as variable communication time-delay and overall system gain, is formulated and serves for the control design and analysis. The performed control synthesis and evaluation are targeting the remote operation where the wireless communication channel cannot secure a deterministic real-time of the control loop. The provided analysis of uncertainties makes it possible to ensure system stability under proper conditions. The theoretically expected results are confirmed through laboratory experiments on the standard industrial hydraulic components.

Index Terms—PID controller, robust control design, hydraulic system, communication delay, remote control, robust stability

#### I. Introduction

Remote wireless operation, with networked control systems, become more crucial in various industries, especially due to more and more spatially distributed sensors, actuators, and different-level controllers, see e.g. a survey provided in [1]. The associated communication constraints, often expressed in varying transmission delays, see e.g. [2], will remain one of the inevitable stumbling block on the way of guaranteeing the stability and desirable level of performance of the feedback control. The latter has to be robust to specific variations in the delays and transmission intervals. Already in early twothousands, the practical investigations were made in remote control of the mechatronic systems over communication networks, see e.g. [3]. At the same time, one can notice the recent works e.g. [4] which prioritize a robust PID design over more sensitive (to uncertainties) compensators of the time-delays, like for example the Smith predictor. The hydraulic drives, often as integrated or even embedded mechatronic systems, are becoming frequently operated in the remote and distributed plants, also via teleoperation and networked control, see e.g. [5]. Having mostly a relatively high level of the process and measurement noise and, at the same time, being safetycritical for several (often outdoor and harsh-environment) applications, also with large forces and corresponding payloads, the hydraulic drives are particularly demanding for a stable operation under the control delays and uncertainties.

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In this paper, one aims to investigate a robust two-degreesof-freedom (2DOF) PID position controller, following the methodology provided in [6] and adapting it to a complex hydraulic drive system with substantial time-delays in the control loop. Here it is worth emphasizing that our goal is not to obtain the best implementation of the remote control, so that to reduce much as possible the RTT (round trip time) in the feedback loop. Instead, one is interested rather in setting up a remotely controlled system with relatively large and variable RTT that makes the system stability more challenging. Moreover, the hydraulic systems are subject to considerable nonlinearities, as it is well known from the subject literature, see e.g. in [7], [8]. This fact makes a robust linear control design particulary challenging and relevant for the practical applications. Here, one purposefully uses the simple 2DOF PID control structure, see e.g. [9], due to its wide spread and acceptance in industries. The recent work provides experimental tests in a laboratory setting, while real industrial hydraulic components like servovalve and linear cylinder are in use. For more details on the experimental laboratory testbed, the reader is referred to [10], [11], while the preliminary and detailed results, which are building fundament for the present work, can be found in [12].

The rest of the paper is organized as follows. Section II provides the control-oriented system modeling while emphasizing: (i) the main steps of a system linearization, (ii) its most crucial uncertainties (including time-delays), and (iii) the resulted perturbed model serving the robust control design approach. Section III is dedicated to the 2DOF PID control design. The experimental results are reported in section IV, while the brief conclusions are drawn in section V.

# II. CONTROL ORIENTED SYSTEM MODELING

### A. Linearized model

First, one analyzes the hydraulic system at hand. Starting from the more physical constitutive equations, a controloriented linear system model is obtained. The hydraulic system is composed of a directional control valve (DCV), i.e. servovalve, and a cylinder. The DCV has a nonlinear behavior due to the dead-zone and saturation of the spool stroke. Also nonlinear friction force appears when moving the piston inside the cylinder chambers. The reduced-order nonlinear model, which results from the full-order nonlinear model (see [13] for details), constitutes the basis for system linearization.

From the reduced-order model of [13] one has the equivalent orifice equation

$$Q_L = zK\sqrt{\frac{1}{2}(P_S - \text{sign}(z) P_L)}, \qquad (1)$$

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where  $Q_L$  is the volumetric flow rate of hydraulic medium, K is the flow coefficient (i.e. which is a valve's constant),  $P_S$  is the supply pressure,  $P_L$  is the system load pressure, and z is an internal variable related to the controlled state of the DCV. Recall that z is subject to the dead-zone and saturation nonlinearities. One linearizes (1) for the fixed  $\hat{P}_L$ ,  $\hat{z}$  using the chain rule. Following to that, one obtains

$$\hat{Q}_L = \hat{C}_q z - \hat{C}_{qp} \hat{P}_L, \tag{2}$$

with

$$\hat{C}_q := \frac{\partial Q_L}{\partial z} \bigg|_{\hat{P}_L} = K \sqrt{\frac{1}{2} (P_S - \operatorname{sign}(\mathbf{z}) \, \hat{P}_L)} , \qquad (3)$$

and

$$\hat{C}_{qp} := -\frac{\partial Q_L}{\partial P_L} \bigg|_{\hat{z}} = \frac{\hat{z}K \operatorname{sign}(\hat{z})}{4\sqrt{\frac{1}{2}(P_S - \operatorname{sign}(\hat{z})P_L)}} \ . \tag{4}$$

In Fig. 1, one can see the block diagram of the linearized system model, from the internal control state z to the output speed  $\dot{x}$  of the cylinder rod. In the block diagram of Fig. 1,

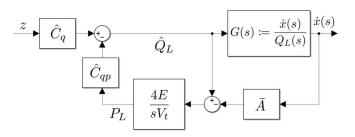


Fig. 1: Block diagram of the linearized process model.

the following transfer function is defined

$$G(s) \coloneqq \frac{\dot{x}(s)}{Q_L(s)} = \frac{1}{(ms + \sigma_{lin})V_t(4\bar{A}E)^{-1}s + \bar{A}}, \quad (5)$$

where m is the total moving mass,  $\sigma_{lin}$  is the equivalent viscous friction coefficient,  $V_t$  is the total oil volume flowing in the hydraulic circuit, E is the bulk modulus, and  $\bar{A}$  is the mean area of the working piston surface of the hydraulic cylinder. Self-evident is that s represents the complex Laplace variable. From the block diagram of Fig. 1, one can directly compute the transfer function from  $Q_L$  to  $P_L$  as

$$R(s) := \frac{P_L(s)}{Q_L(s)} = \frac{4E(1 - G(s)\bar{A})}{sV_t} = (ms + \sigma_{lin})G(s)\bar{A}^{-1}.$$

Hence, the transfer function from z(s) to  $\dot{x}(s)$  results in

$$\hat{G}(s) := \frac{\dot{x}(s)}{z(s)} = \frac{\hat{C}_q G(s)}{1 + \hat{C}_{qp} R(s)} . \tag{7}$$

Important to notice is that  $\sigma_{lin} > 0$  is used in (5) and (6) in order to describe the linear viscous friction behavior. An appropriate choice of  $\sigma_{lin}$  appears relevant because the real frictional behavior is strongly nonlinear, as confirmed with identification data shown below. Indeed, one can recognize

in the velocity-force coordinates in Fig. 2, the experimentally collected data points [10] for both motion directions. Note that the points are determined each from the steady-state measurement of relative velocity  $\dot{x}$  and load pressure at the unidirectional drive experiments with a nearly constant speed. Recall that at steady-state, the load pressure is proportional to the total resistive force, which is due to the total friction when no other forces are in balance. The experimental data are also fitted with the Stribeck friction model, see e.g. [14, eq. (2)], which is then used for the sake of a more accurate numerical simulation. The dashed line in Fig. 2 reflects the selected linear friction coefficient  $\sigma_{lin}$ . This is chosen so that the linear model reaches the same friction force level towards the end of the considered velocity range. At the same time, for the maximal possible relative velocity  $\dot{x}_{max} = 0.25 \left[ \frac{m}{s} \right]$ , detected in the open-loop experiments, the  $\sigma_{lin}$  constitutes a trade-off which minimizes an integral square error between the identified Stribeck and linear viscous friction model.

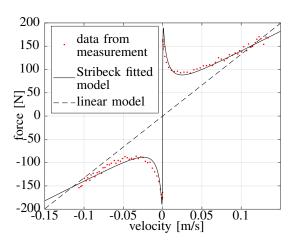


Fig. 2: Comparison between experimental and model data.

Now, the obtained linear model (7) is augmented by the overall communication time delay  $\tau$ . Therefore, one derives the overall process transfer function, i.e. from the delayed control channel z to the output position of interest x, as

$$P(s) := \frac{x(s)}{z(s)}e^{-s\tau} = \hat{G}(s)s^{-1}e^{-s\tau} . \tag{8}$$

Since the overall plant model has two gaining factors related to the linearization, cf. (3), (4), and one weakly-known time delay factor, one has to deal with a *nominal process transfer function*, for which one fixes the nominal parameter values  $\tau_{\text{nom}}$ ,  $C_{q,\text{nom}}$ ,  $C_{qp,\text{nom}}$ . Later, those parameters are considered as a source of uncertainties in the robust control design. The nominal process transfer function is given explicitly by

$$P_{\text{nom}}(s) = \frac{e^{-s\tau_{\text{nom}}} \frac{C_{q,\text{nom}}\bar{A}}{\sigma_{lin}C_{qp,\text{nom}} + \bar{A}^2}}{s \left[ s^2 \frac{mV_t}{4E(\sigma_{lin}C_{qp,\text{nom}} + \bar{A}^2)} + s \frac{C_{qp,\text{nom}}m + \frac{\sigma_{lin}V_t}{4E}}{\sigma_{lin}C_{qp,\text{nom}} + \bar{A}^2} + 1 \right]} . \tag{9}$$

#### B. Uncertainties analysis

As shown above, the linearized gaining factors  $C_q$  and  $C_{qp}$  depend on the input and state operating points  $\hat{z}$  and  $\hat{P}_L$ , respectively. On the other hand, the communication delay can be of a purely stochastic nature, and the only upper bound  $\tau_{\rm max}$  can be assumed. In order to assign the nominal values of the uncertain parameters, consider the following.

• In Fig. 3, the  $C_{qp}(P_L,z)$  surface is shown for the sake of visualization. Since the  $C_{qp}$ -surface is not uniformly distributed but symmetrical with respect to the  $(P_L,z)$ -origin, one proper choice of the nominal value is the integral mean value over the whole operative ranges, i.e.  $z \in (-1,+1)$  and  $P_L \in (-P_s,+P_s)$ . As it is visible from eq. (4),  $\forall z \in [-1,1] \lim_{P_L \to P_s} C_{qp}(P_L,z) \to +\infty$ , so that one can stop integration at e.g. 95 % of  $P_s$ , which is an appropriate range for the load pressure  $P_L$ . In a similar way as  $C_{qp}$ , one can then assert the value for  $C_q$ .

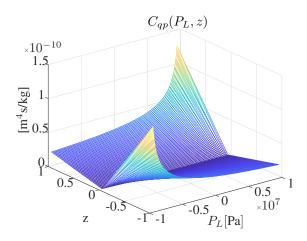


Fig. 3: Variations of the gaining factor  $C_{qp}(P_L, z)$ .

• In order to analyze the (RTT) delay  $\tau$ , more than 10 different communication experiments on the hardware of experimental testbed were performed. The spatial distance between the routers of a wireless network and the intensity of the exchanged data were varied. In Fig. 4, a typical distribution determined from the measurements of  $\tau$  is shown. Note that the 0.01 [s] column-width of the histogram corresponds the 0.01 [s] quantization of  $\tau$ , the latter due to the communication time period captured on side of the remote controller. As can be found in the literature, see e.g. [15], [3], an RTT model for TCP/IP communication often suggests the  $\gamma$ -distribution. From Fig. 4, one can recognize that the fitted  $\gamma$ -distribution is well in accord with the measurement. Based on the determined  $\gamma$ -distribution, the nominal value  $\tau_{nom}$  is calculated as average by evaluating the integral mean value.

#### C. Perturbed system model

The perturbed system model is defined as following

$$P_{\tau}(i\omega) = \left[1 + \Delta_U(i\omega)W_U(i\omega)\right]P_{\text{nom}}(i\omega) , \qquad (10)$$

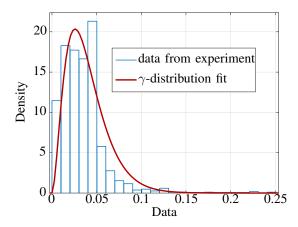


Fig. 4:  $\gamma$ -distribution fit of the measured  $\tau$  distribution.

where  $W_U(i\omega)$  is a fixed stable transfer function for weighing the uncertainties, and  $\Delta_U(i\omega)$  is a variable stable transfer function satisfying  $\|\Delta_U(i\omega)\|_{\infty} < 1$ . The complex number and angular frequency are denoted by i and  $\omega$ , correspondingly. The used structure model is very well known as *multiplicative* perturbation. Indeed, the transfer characteristics  $P_{\tau}(i\omega)$  could additionally vary from the nominal one in a range defined by  $\Delta_U(i\omega)W_U(i\omega)$  in the magnitude, and by  $\Delta_U(i\omega)$  in the phase. One chooses the multiplicative perturbation structure to represent the uncertain system because of the following reasoning. From eq. (9), one can recognize that the nominal transfer function has a pair of conjugate-complex poles and a free integrator. The transfer function parameters, related to the pole pair, are the gaining factor, natural frequency, and damping coefficient

$$k(\hat{C}_q, \hat{C}_{qp}) = \frac{\hat{C}_q \bar{A}}{\sigma_{lin} \hat{C}_{qn} + \bar{A}^2} , \qquad (11)$$

$$\omega_n(\hat{C}_{qp}) = \sqrt{\frac{4E(\sigma_{lin}\hat{C}_{qp} + \bar{A}^2)}{mV_t}} , \qquad (12)$$

$$\xi(\hat{C}_{qp}) = \frac{\hat{C}_{qp}m + \frac{\sigma_{lin}V_t}{4E}}{\sigma_{lin}\hat{C}_{ap} + \bar{A}^2} \cdot \frac{\omega_n}{2} . \tag{13}$$

respectively. Following to that, one can compute the maximum relative deviation for these three parameters, which are varying subject to linearization. This is done by iterative calculation of (11), (12), (13) over the range of possible  $(C_{qp}, C_q)$  values, followed by a comparison with the parameter values obtained for the nominal  $(C_{qp,nom}, C_{q,nom})$ . This results in

$$\begin{array}{l} \text{max relative deviation} \left[k(C_{qp},C_q)\right] = 71.37\% \;, \\ \\ \text{max relative deviation} \left[\omega_n(C_{qp},C_q)\right] = 6.1\% \;, \\ \\ \text{max relative deviation} \left[\xi(C_{qp},C_q)\right] = 25.1\% \;. \end{array} \tag{14}$$

One can recognize that the maximal possible deviation on  $\left[k(C_{qp},C_q)\right]$  is significantly larger comparing to the maximal deviations of  $\left[\omega_n(\hat{C}_{qp})\right]$  and  $\left[\xi(\hat{C}_{qp})\right]$ . Such dominance

in the gain variation justifies the multiplicative perturbation assumption made for the present system.

A sufficient robust stability condition for the model with the multiplicative perturbation, following to e.g. [16], is

$$||W_U(i\omega)T(i\omega)||_{\infty} < 1 , \qquad (15)$$

where  $T(i\omega)$  is the closed-loop transfer function. One can easily see that the robust stability (15) depends on the weighting function  $W_U(i\omega)$ . Since it has to satisfy the condition (10), one can write

$$\left| \frac{P_{\tau}(i\omega)}{P_{\text{nom}}(i\omega)} - 1 \right| \le \left| W_U(i\omega) \right| \,. \tag{16}$$

Since the multiplicative perturbation differs the  $P_{\tau}$  and  $P_{\text{nom}}$  transfer functions by exactly the gaining factor and time-delay element, the inequality (16) can be transformed into, cf. [16],

$$|ke^{-\tau i\omega} - 1| \le |W_U(i\omega)| . \tag{17}$$

In order to satisfy (17) for all possible  $C_q$ ,  $C_{qp}$ , and  $\tau$  in the range of variations, consider the available upper bounds  $k_{\rm max}$  and  $\tau_{max}$ . Then, one needs to find a stable transfer function  $W_U(i\omega)$  which can guarantee the inequality (17) holds for the  $(k_{\rm max},\tau_{max})$  pair, so that it remains valid also for all  $0 < k < k_{\rm max}$  and  $0 < \tau < \tau_{\rm max}$ . Assuming the second-order lead transfer function

$$W_U(s) = k_w \frac{\frac{s^2}{\omega_z^2} + 2\xi_z \frac{s}{\omega_z} + 1}{\frac{s^2}{\omega_z^2} + 2\xi_p \frac{s}{\omega_p} + 1} , \qquad (18)$$

as the weighting function for robust stability (15), the parameter values  $\omega_{z,p}$ ,  $\xi_{z,p}$ , and  $k_w$  are fitted by minimizing the square error between  $W_U(i\omega)$  and the left-hand-side of (17) for a certain range of angular frequencies around both corner frequencies  $\omega_z < \omega_p$  of the lead element (18).

#### III. CONTROL DESIGN

The control design follows the methodology provided in [9], [6]. The control objectives to be achieved are:

- 1) fast load disturbance response;
- 2) robustness against the model uncertainties;
- 3) robustness against the measurement noise;
- 4) set point response accuracy.

The control solution includes the following measures:

- 1) maximize the integral action of the PID controller;
- 2) define a robust constraint;
- 3) apply the second-order filter  $F_n(s)$  to feedback;
- 4) tune the set point parameter b and filter  $F_{sp}(s)$ .

# A. Robust feedback design

The applied design algorithm [9] maximizes the integral action  $k_i$  of the standard PID feedback controller

$$C_c(s) = k_p + \frac{k_i}{s} + sk_d , \qquad (19)$$

satisfying the constraint

$$f(k_p, k_i, k_d, \omega) = \left| \left[ k_p + i(k_d \omega - k_i/\omega) \right] P_{\text{nom}}(i\omega) + 1 \right|^2 \ge r^2.$$
(20)

The inequality (20) guarantees that the open-loop transfer function  $C_c(i\omega)P_{\rm nom}(i\omega)$  lays outside the circle of the radius r, which is centered in(-1,i0) of the complex plane. Then, it is the Nyquist theorem which guarantees the stability of the closed-loop system under this condition. Therefore, the system remains stable until  $C(i\omega)P_{\rm nom}(i\omega)$  surrounds (-1,0). The parameter r describes the robustness of the system and (20) is called a robust constraint.

If looking at the definition of the infinite norm of the sensitivity function S, cf. [17], which is the maximum absolute value of  $S(i\omega)$  over all frequencies  $\omega$ , i.e.

$$M_s := \max_{\omega} |S(i\omega)| = \max_{\omega} \left| \frac{1}{1 + P_{\text{nom}} C_c(i\omega)} \right|,$$
 (21)

one can write  $r = \frac{1}{M_s}$ . Then, one can choose a value of  $M_s$  according to the robustness required from the feedback control system. One assumes  $M_s = 1.1$ , cf. [9], in accord with a relatively high level of perturbations in the system.

For the identified nominal process

$$P_{\text{nom}}(s) = e^{-0.03s} \frac{8.255 \cdot 10^5}{s \left[ s^2 + 948s + 2.219 \cdot 10^6 \right]} , \qquad (22)$$

one obtains the following control gains

$$k_p = 12.7534$$
,  
 $k_i = 31.1783$ ,  
 $k_d = 0.1472$ .

by applying the  $k_i$  maximization algorithm proposed in [9]. In Fig. 5, one can verify the Nyquist plot of the open-loop transfer function with respect to the above robust constraint. In particular, one can see that the algorithm maximizes the PID parameters until reaching the robust constraint, i.e. by touching the r-circle at three points  $P_1$ ,  $P_2$ ,  $P_3$ , i.e. at three different angular frequencies. The resulted robust feedback control, designed for the nominal process, can be further assessed on the robust stability (15). Here, the closed-loop transfer function  $T(i\omega) = P_{\text{nom}}C_c(i\omega)\left(1 + P_{\text{nom}}C_c(i\omega)\right)^{-1}$  is multiplied with  $W_U(i\omega)$ , which is satisfying (17) for  $\tau = \tau_{\text{max}}$ . Worth noting is that while  $\tau_{\text{nom}} = 0.03$ , its upper bound  $\tau_{\text{max}} = 0.11$ , cf. Fig. 4, is still satisfying the robust stability (15).

# B. 2DOF control structure

In Fig. 6, the overall 2DOF control structure is shown with

$$G_{\rm ff}(s) = bk_p + \frac{k_i}{s} \,, \tag{24}$$

$$F_{\rm n}(s) = \frac{1}{(1 + \frac{s}{2N\omega_{\rm o}})^2} ,$$
 (25)

which are the feed-forward and feed-back filters, respectively. Here b is the set-point parameter to be tuned, and N is the parameter of the noise cutoff frequency to be adjusted for having a suitable feedback response. N=5 is set as an appropriate value, cf. [6]. D(u) is the inverse map of the orifice dead-zone, cf. [10], which has to compensate the static non-linearity which was not considered in the nominal process  $P_{\text{nom}}(s)$ . Further, compute the pre-filter, cf. [6],

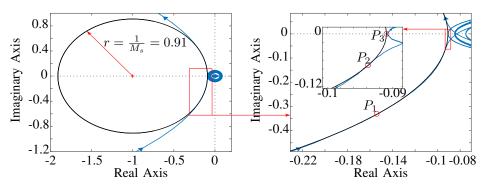


Fig. 5: Nyquist diagram of the open loop transfer function with PID controller designed with (23).

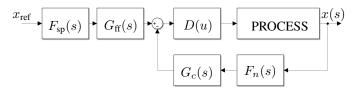


Fig. 6: Block diagram of the 2DOF control structure.

$$F_{\rm sp}(s) = \frac{1}{1 + s \frac{2\pi}{\omega_{\rm sp}} \sqrt{M_w^2 - 1}} = \frac{1}{1 + s\tau_{\rm sp}} ,$$
 (26)

so as to guarantee that  $\max_{\omega} \big[|W(i\omega)|\big] \leq 1$ , where  $M_w = \max_{\omega} [|W(i\omega)|]$ , and

$$W(s) = \frac{x(s)}{x_{\text{ref}}(s)} = \frac{G_{\text{ff}}P_{\text{nom}}(s)}{1 + G_{\text{c}}F_{\text{n}}P_{\text{nom}}(s)} . \tag{27}$$

This way, the overall closed-loop transfer function, from the reference position to the output rod position, will have  $M_w = 1$ , hence, ensuring no overshoot in the step response.

# IV. EXPERIMENTAL RESULTS

The robust 2DOF controller, developed according to sections II and III, is experimentally evaluated on the laboratory testbed [10]. The used experimental setup is shown in Fig.



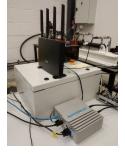


Fig. 7: Laboratory experimental setup: hydraulic testbed [10] on the left; switch cabinet with the embedded hardware interfaces, real-time board, and WiFi routers on the right.

7. The real-time SpeedGoat board is controlling the power and sensor interfaces, with deterministic sampling time set to

0.0005 sec. The SpeedGoat board is connected to a standard WiFi router as a point-to-point TCP/IP communication, this way sending the measured output values, received from the sensor, and receiving the control values from a remote PC-based controller. The remote PC-based controller is realized on a standard conventional laptop computer. Due to non-real-time processes of the TCP/IP-based socket and implemented control on the running PC, the minimal possible time delay  $\tau_{\rm min}=0.01$  sec appears as a communication sample time.

Two communication scenarios have been evaluated: (i) the remote control communication performs via a point-to-point Ethernet connection between the real-time SpeedGoat and PC-based controller; (ii) the remote control communication performs via a wireless connection between the real-time SpeedGoat and PC-based controller by means of WiFi. Note that for (ii), various spatial distances between the WiFi communicating nodes were tested. In both communication scenarios, the RTT delay, which corresponds to the overall  $\tau$ , was monitored and recorded in the feedback loop.

The results shown below visualize the reference and output position of the hydraulic cylinder, together with the recorded time delay in the upper plots, and the corresponding control signal in the lower plots. A series of square-pulse-shaped (with 0.1 m amplitude) positioning experiments are shown for communication scenario (i) in Fig. 8. Note that for time-delay values higher than 0.11 sec, cf. sections II and III, an instability can occur. Further it is noted that the smoothing set-point filter (26) is not applied at that stage. The same type positioning experiments for the communication scenario (ii) are shown in Fig. 9. Note that despite  $\tau$  is transiently exceeding the  $\tau_{\rm max}$ value, the robustly designed 2DOF PID control maintains a stable and performant response, with solely shortcoming of transient oscillations. In Fig. 10, the communication scenario (ii) is shown when additionally applying the set-point filter (26), cf. Fig. 6. This way, the square-pulse-shaped reference  $x_{\text{ref}}$  is additionally lagged, which slows down the overall output response but, in return, avoids the transient oscillations. Worth noting is that the increased spatial distance between the WiFi nodes led to the larger  $\tau$ -variations in this case, with more frequent values closer to  $\tau_{\rm max}$ , cf. Figs. 8, 9, and 10.

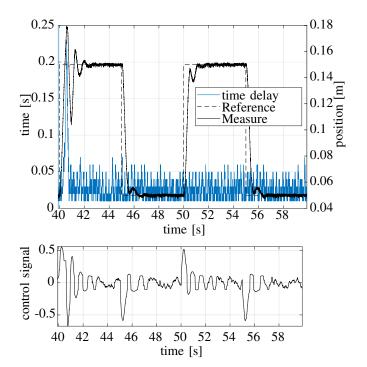


Fig. 8: Experimental control response (Ethernet connection).

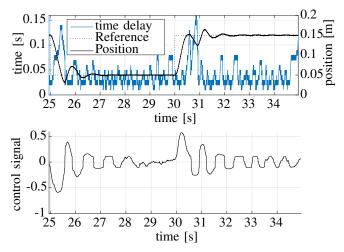


Fig. 9: Experimental control response (WiFi connection).

# V. CONCLUSIONS

This paper shows the application of the linear 2DOF control methodology [9] to the nonlinear uncertain hydraulic drive system with significant time delays due to the wireless remote control. The robust constraint on the varying system gain and time delay parameters were specified and used for the feedback control design that meets the robust stability criteria for multiplicative disturbances. It is demonstrated in the laboratory experiments, accomplished on the standard industrial components, that the robust 2DOF PID control is well applicable to remotely operated hydraulic drives with only output measurement of the cylinder stroke.

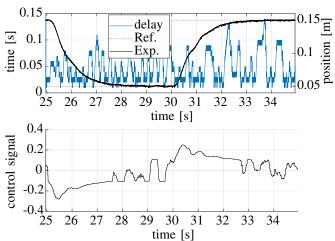


Fig. 10: Experimental control response, using additionally the set-point filter (26) (WiFi connection).

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