

## Article

# Simple Lossless Inductive Snubbers-Assisted Series Load Resonant Inverter Operating under ZCS-PDM Scheme for High-Frequency Induction Heating Fixed Roller

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**Abstract:** This paper presents a high-frequency pulse-density-modulated (PDM) soft-switching series load resonant inverter for use in induction heating (IH) fixed roller applications, which is used in copy and printing machines. The proposed simple high-frequency resonant inverter uses an asymmetrical pulse pattern PDM control scheme to achieve complete zero-current soft-switching commutations over a wide output range of input power regulation. Additionally, when the printer toner requires operation in very light load conditions, this causes difficulty in achieving zero-voltage or zero-current soft-switching operations in the IH high-frequency resonant inverters with pulse frequency modulation or pulse width modulation control schemes. The proposed resonant inverter demonstrates the capability to accomplish highly efficient power conversions. In this work, a fixed roller for printing machines is developed for doing experiments to verify the efficiency of the proposed circuit topology and its PDM control schemes. The inverter's steady-state and transient operating principles are analyzed based on the proposed control strategy at a high-frequency PDM. Operating conditions such as power loss analysis, power conversion efficiency and temperature rise characteristics of the proposed inverter are presented and analyzed through experimental results. Finally, from a practical viewpoint, a comparative study of a conventional halogen lamp heater and the proposed IH fixed roller is deliberated.

**Keywords:** induction heating; zero-current soft-switching; pulse density modulation; high-frequency induction heating fixed roller



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## 1. Introduction

In recent years, power-electronics-based power conditioning devices have been used in the area of induction heating (IH) technologies. IH technologies are energy efficient [1], and they are used extensively for heating applications (e.g., cooking stoves, etc.) [2,3]. IH is also used in office automation appliances. IH systems are fundamentally composed of electrical power converter circuits, digital control schemes and magnetic components [4]. There are different types of circuit topology for IH applications. Most of them are categorized as full-bridge inverters [5,6], half-bridge inverters [7–11], resonant single-ended inverters [12] and inverters employing active voltage clamping [13]. The half-bridge inverters are widely used for IH applications due to their cost effectiveness and robustness. Additionally, the

techniques of zero-voltage and zero-current soft-switching (ZVS, ZCS) are employed in the circuit topologies, resulting in the reduction of losses during switching [8,14].

Generally, pulse modulation methodology is employed in the high-frequency inverter to achieve output power regulation for IH application. Mainly, there are three types of modulations, which are as follows: (i) pulse frequency modulation (PFM) [15,16], (ii) pulse width modulation (PWM) [17] and (iii) pulse density modulation (PDM) [18–21]. The simplest modulation technique is PFM. Hence, it is the most widely employed with a single-switched inverter, and a variable switching frequency is used for controlling the injected currents from the voltage power source. However, the variation of the switching frequency for control of the IH load parameters is a disadvantage for domestic applications. As a result, the inverters with PFM-controlled schemes emit some annoying acoustic sounds [22]. By contrast, the sound of inverters with PWM-controlled schemes is quieter. However, the power conversion efficiency of PWM inverters is lower when they are operated at low power output due to soft-switching commutations, which are likely to fail [23].

In order to improve the functionality and efficiency of both conventional PFM and PWM high-frequency resonant inverters, PDM control schemes have been widely used in recent years. Most early works on implementing PDM control schemes in high-frequency resonant inverters are usually for industrial applications [24]. These inverters are proven to be effective because they are operated with fixed operating frequency, which guarantees the achievement of soft-switching operations at a wider range of output power. Generally, the power requirement of domestic IH applications is less than 2 kW, though this needs further investigation with different control topologies. There are some efforts towards implementing PDM into various modulation control schemes so that high-frequency resonant inverters can be operated in dual modes with the PDM operations at low-output-power regulations [18,25–28]. Such techniques significantly improve the efficiency of high-frequency resonant inverters. As a result, ZCS and ZVS operations are used at a wider range of output power, especially when power output is lower. An effort to improve high-frequency resonant inverter operation at low power output uses the discontinuous mode to establish the soft-switching commutations at a lower power output range [7]. It demonstrates improvement in the efficiency of general domestic IH applications at a 1.5 kW power range. However, the control schemes of discontinuous current mode are similar to PDM, and they need the switching frequency to be changed regularly in accordance with the required output power. They may result in the failures of soft-switching operations at a very low power range.

Typically, in conventional copy and printing machines, halogen lamp heater radiant heat is used for the process of toner fixing. However, it is not an effective method due to a low conversion efficiency and heat response since it uses an indirect heating process. However, these disadvantages can be overcome using the IH process, with the benefits of the eddy currents and magnetic hysteresis. The IH process is obviously a direct heat induction with accurate control in its power requirement. Additionally, printing and copy machine operation requires a wide range of power regulation, as they are required to undergo rated power operations ranging from low output (as low as their stand-by mode) up to their maximum power output.

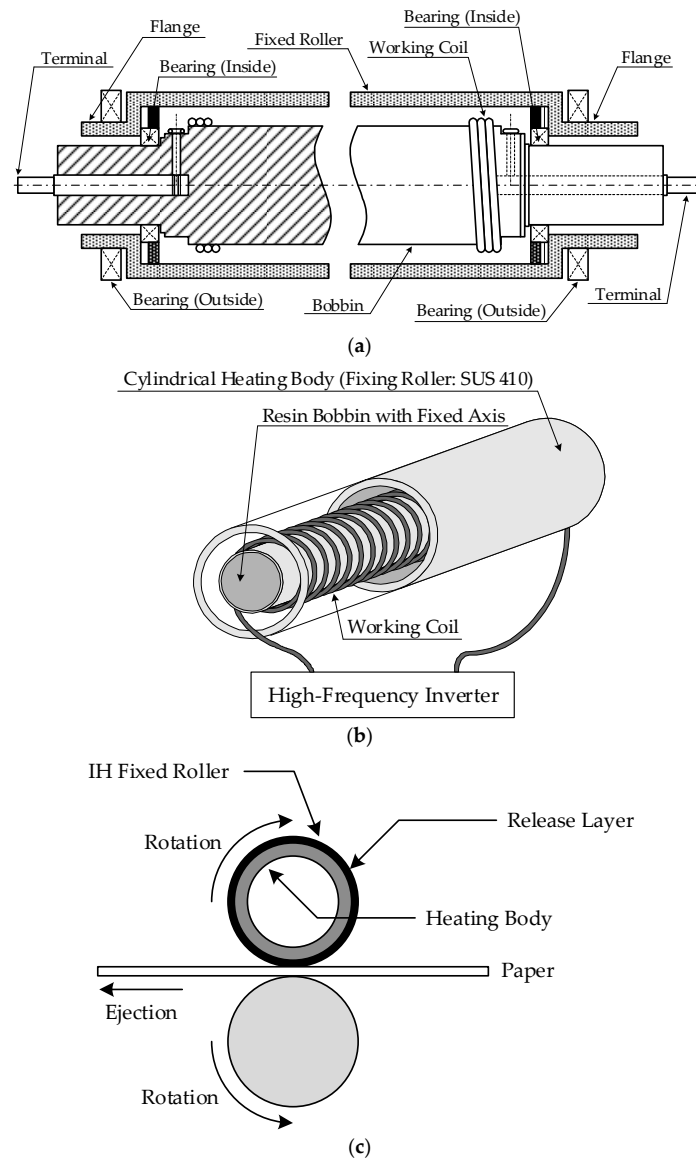
The key focus of this paper is to use IH rollers in printing and copy machines by applying a PDM-controlled inverter using high-frequency series load resonant soft-switching technology. The PDM control scheme of this circuit topology is operated under the asymmetrical pattern of pulses. The symmetrical PDM pattern is used in high-power applications [24]. The extremely low-power-output operations, such as in the stand-by mode of a copy machine, can be realized using an asymmetrical PDM pattern. Additionally, this paper presents an interesting circuit topology, using only one auxiliary resonant capacitor with the aids of two separated auxiliary resonant inductors. The presented circuit topology, with the help of fixed-switching operating frequency and the PDM control scheme, enhances the combinations of ZVS and ZCS operations. The circuits of power regulation and operational characteristics are analyzed based on the developed experimental setup and obtained results. Additionally, loss calculations and power conversion efficiencies are

analyzed. Lastly, a conventional halogen lamp heater and the proposed IH fixed roller application are presented from a practical viewpoint.

## 2. Schematic of Induction Heating Fixed Roller and Its Equivalent Circuit

### 2.1. Schematic Structure of Induction Heating Fixed Roller

An IH-based fixed roller for printing and copy machines is specially developed in a laboratory. This fixed roller uses IH and directly heats the external roller to the printing toner. This directly heated IH-based fixed roller is highly efficient in comparison to indirect radiant heat generated by the use of a halogen lamp, which is conventionally used. Further, an IH fixed roller's surface temperature (160–200 °C) can be easily controlled. Fixed roller structure is shown in Figure 1a,b. The IH fixed roller is composed of a rolling drum with a heating coil wound around an internal resin bobbin. Figure 1c illustrates an IH fixed roller toner fixing process. Surfaces of an aluminum or iron heating body have a release layer. This layer is composed of either a soft type with an elastic body or a hard type with a resin. Full-color printing and copy uses the soft type, and mono-color uses the hard type. Magnetic stainless steel (SUS 410) is used in the heating body. Carbon ceramic or an alloy of titanium can also be used.

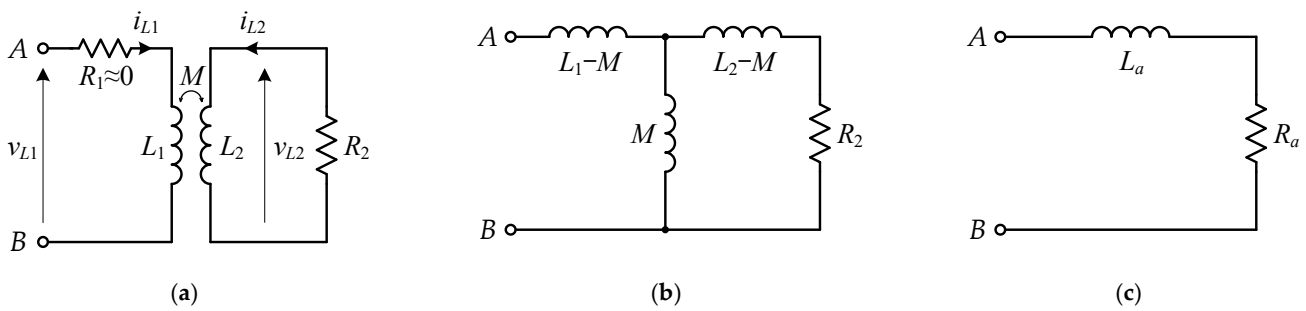


**Figure 1.** Induction heating fixed roller for copy and printing machines. (a) Sectional view. (b) Internal configuration. (c) Toner fixing process.

### 2.2. Transformer Circuit Model for IH Load

The conventional  $R$ - $L$  series or parallel model for IH applications uses equivalent impedance models. However, the practical model of IH applications requires distorted voltage and current to be applied to the IH load in case of operation with a high-frequency inverter. In order to analyze and simulate the characteristics of a high-frequency inverter, including IH load, an analytical model of the real IH load is required.

Time-varying load parameters are used in IH load applications requiring high temperatures. Applications such as thermal processing, heat treatment and metal melting use these time-varying load parameters. However, in the case of applications for low temperatures, load parameters vary slowly around an operating point. Hence, in this work, load parameters are considered to be constant. To provide an accurate representation of the IH load, the transformer model is used for simulation analysis, as shown in Figure 2a. The model of the transformer has self-inductances  $L_1$  and  $L_2$ , the winding resistance  $R_1$  and the effective resistance  $R_2$ , considering the skin effect of the heating object. The equivalent circuit parameters of Figure 2a are assumed to be constant as the quasi-steady state. Resistance  $R_1$  is small enough and uses the litz wire, which reduces the skin effect, and therefore, it is ignored. Resistance  $R_2$  is based on the current penetration depth, and the skin effect is related to the high-frequency inverter switching frequency.



**Figure 2.** Transformer circuit model for IH fixed roller. (a) Transformer model. (b) Transformer equivalent circuit model. (c)  $L$ - $R$  series equivalent circuit model.

The state equation for the equivalent circuit of the IH load in Figure 2a is expressed as follows:

$$\begin{cases} L_1 \frac{di_{L1}}{dt} + M \frac{di_{L2}}{dt} = v_{L1} \\ M \frac{di_{L1}}{dt} + L_2 \frac{di_{L2}}{dt} + R_2 i_{L2} = 0 \end{cases} \quad (1)$$

Magnetic fluxes  $\varphi_1$  and  $\varphi_2$  are expressed as follows:

$$\begin{cases} \varphi_1 = L_1 i_{L1} \\ \varphi_2 = M i_{L2} \end{cases} \quad (2)$$

By substituting  $\varphi_1$  and  $\varphi_2$  from Equation (2) into Equation (1), the following equation can be obtained:

$$\begin{cases} \frac{d\varphi_1}{dt} + \frac{d\varphi_2}{dt} = v_{L1} \\ k^2 \frac{d\varphi_1}{dt} + \frac{d\varphi_2}{dt} + \frac{\varphi_2}{\tau} = 0 \end{cases} \quad (3)$$

where

$$\tau = \frac{L_2}{R_2} \quad (4)$$

$$k = \frac{M}{\sqrt{L_1 L_2}} \quad (5)$$

By solving Equation (3), the IH load parameters can be represented by the electromagnetic coefficient of coupling  $k$  and time constant  $\tau$  of the high-frequency inverter. This inverter operation for an IH load is independent of the values of  $R_2$  and  $L_2$  if these values'

ratio is constant for a certain value of  $k$ . The electromagnetic coupling degree with the heating coil and the heating body is represented by the parameter  $k$ . The IH load time constant is represented by parameter  $\tau$ . The  $L_1$  value is the heating coil self-inductance as measured on the transformer model primary side, with the secondary side open-circuited. Further, this  $L_1$  value equals the heating coil self-inductance with a heating object with zero conductivity and a nonmagnetic heating body under the no-load condition using materials such as stainless steel or aluminium.

### 2.3. Theoretical Analysis of IH Load Parameters

This section describes the theoretical analysis of the parameters  $\tau$  and  $k$  derived by the equivalent circuit expression on the above and actual measurement of these parameters. The transformer equivalent circuit model can be illustrated in Figure 2b. We can only measure the self-inductance  $L_1$ , the equivalent inductance  $L_a$  and the equivalent resistance  $R_a$ , as shown in Figure 2c.

From Figure 2b, the equivalent impedance of terminal A-B is expressed by the following equation:

$$\begin{aligned} Z_{AB} &= j\omega(L_1 - M) + \frac{j\omega M[R_2 + j\omega(L_2 - M)]}{j\omega M + R_2 + j\omega(L_2 - M)} \\ &= \frac{\omega^2 M^2 R_2}{R_2^2 + \omega^2 L_2^2} + j\omega \frac{L_1 R_2^2 + \omega^2 L_2 (L_1 L_2 - M^2)}{R_2^2 + \omega^2 L_2^2} \end{aligned} \tag{6}$$

where  $\omega$  is angular frequency.

The impedance of the L-R series equivalent circuit model in Figure 2c is expressed as follows:

$$Z_{AB} = R_a + j\omega L_a \tag{7}$$

Because the real part and the imaginary part of Equations (6) and (7) are equal, the equivalent resistance  $R_a$  and inductance  $L_a$  can be expressed as follows:

$$\begin{cases} R_a = \frac{\omega^2 M^2 R_2}{R_2^2 + \omega^2 L_2^2} \\ L_a = \frac{L_1 R_2^2 + \omega^2 L_2 (L_1 L_2 - M^2)}{R_2^2 + \omega^2 L_2^2} \end{cases} \tag{8}$$

$L_1 - L_a$  can be calculated as follows:

$$L_1 - L_a = \frac{\omega^2 L_2 M^2}{R_2^2 + \omega^2 L_2^2} \tag{9}$$

From Equations (8) and (9),  $\tau$  and  $k$  can be described with  $L_1$ ,  $L_a$  and  $R_a$  as follows:

$$\tau = \frac{L_2}{R_2} = \frac{L_2}{R_2} \times \frac{\frac{\omega^2 M^2}{R_2^2 + \omega^2 L_2^2}}{\frac{\omega^2 M^2}{R_2^2 + \omega^2 L_2^2}} = \frac{\frac{\omega^2 L_2 M^2}{R_2^2 + \omega^2 L_2^2}}{\frac{\omega^2 M^2 R_2}{R_2^2 + \omega^2 L_2^2}} = \frac{L_1 - L_a}{R_a} \tag{10}$$

$$k = \frac{M}{\sqrt{L_1 L_2}} = \sqrt{\frac{M^2}{L_1 L_2}} = \sqrt{\frac{M^2}{L_1 L_2}} \times \frac{\sqrt{\frac{\omega^4 M^2 (R_2^2 + \omega^2 L_2^2)}{(R_2^2 + \omega^2 L_2^2)^2}}}{\sqrt{\frac{\omega^4 M^2 (R_2^2 + \omega^2 L_2^2)}{(R_2^2 + \omega^2 L_2^2)^2}}} = \sqrt{\frac{R_a^2 + \omega^2 (L_1 - L_a)^2}{\omega^2 L_1 (L_1 - L_a)}} \tag{11}$$

As a result, IH load can be expressed by three parameters,  $L_1$ ,  $\tau$  and  $k$ .

## 3. ZCS Series Load Resonant High-Frequency Inverter Employing PDM Control

### 3.1. Circuit Description

A series load resonant high-frequency soft-switching inverter employing PDM control for an IH fixed roller is shown in Figure 3. It is composed of  $S_1$  and  $S_2$  active power switches;  $C_r$ , a resonant capacitor in series with IH load; and  $L_{S2}$  and  $L_{S1}$ , two ZCS-assisted snubber inductors, which are in series with  $S_1$  and  $S_2$ , respectively.

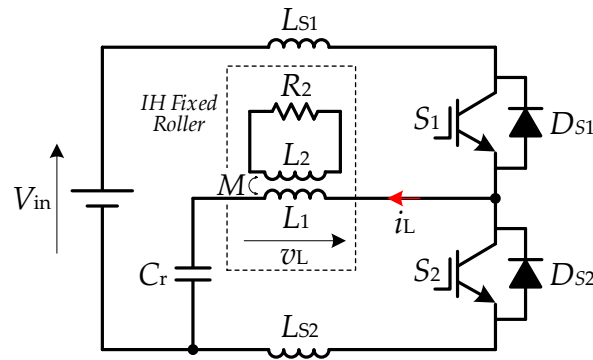


Figure 3. Series load resonant high-frequency soft-switching inverter.

3.2. Principle of Operation

PDM control with gate pulse sequences of the proposed high-frequency inverter is illustrated in Figure 4. Basically, it is operated under either a power-supplying condition or an idling condition. Switching pulse numbers in the period of the PDM determines the output power.  $D_{PDM}$ , the PDM duty ratio, is described as follows:

$$D_{PDM} = \frac{T_{on}}{T_{on} + T_{off}} = \frac{T_{on}}{T_{PDM}} \tag{12}$$

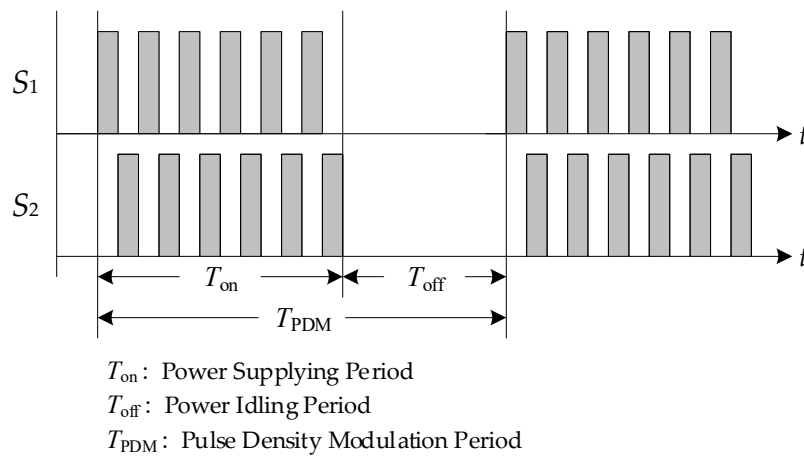


Figure 4. PDM control gate pulse sequences.

The auxiliary snubber inductors  $L_{S1}$  and  $L_{S2}$  allow soft-switching ZCS commutation for the active power switches  $S_1$  and  $S_2$ , which provide the overlapping current mode in  $S_1/D_{S2}$  and  $S_2/D_{S1}$  when they are in the continuous load current mode. The range of ZCS of the proposed inverter covers all ranges of inverter power regulation. Additionally, the commutation of the ZCS theoretically causes the IGBTs to have zero tail current. Thus,  $S_1$  and  $S_2$  in the proposed inverter have extremely low switching power losses. Furthermore, power losses are non-existent in this PDM scheme during the non-injected power period compared with the series load resonant inverters employing control methods such as PFM and PWM in light load conditions.

3.3. Operation of the Circuit

The proposed soft-switching inverter circuit mode transitions for the IH fixed roller are shown in Figure 5a. Figure 5b shows the current and voltage waveforms in each mode of operations. Each mode of operating principle is explained as:

Mode 1 With switch  $S_1$  in the conduction mode, the power is delivered to the resonant capacitor  $C_r$ , snubber inductor  $L_{S1}$  and the IH load. The attenuated sinusoidal resonance starts through the IH load.

- Mode 2 When load current  $i_L$  decreases through  $S_1$  to zero at  $t = t_1$ , anti-parallel diode  $D_{S1}$  is naturally turned on. At turn-off transition, this results in  $S_1$  achieving complete ZCS-and-ZVS hybrid soft commutation.
- Mode 3 While diode  $D_{S1}$  is in conducting mode, the  $S_2$  switch turns on at  $t = t_2$ . Consequently, the  $D_{S1}$  current commutates to  $S_2$ . Eventually, the  $D_{S1}$  current is completely transferred to switch  $S_2$  by snubber inductor  $L_{S2}$ . Therefore, switch  $S_2$  achieves ZCS turn-on.
- Mode 4 While switch  $S_2$  is still in conduction mode, the diode  $D_{S1}$  current becomes zero at  $t = t_3$ . Then,  $C_r$  delivers the output power to the IH load. This results in the attenuated sinusoidal resonance starting through the IH load.
- Mode 5 As the load current  $i_L$  increases, the  $S_2$  current decreases to zero at  $t = t_4$ . As a result, anti-parallel diode  $D_{S2}$  is naturally turned on and  $S_2$  turns off by complete ZVS and ZCS throughout this operating mode.
- Mode 6 While diode  $D_{S2}$  is still in conduction mode, switch  $S_1$  turns on at  $t = t_5$ . The  $D_{S2}$  current begins to commutate to switch  $S_1$ . Eventually, the  $D_{S2}$  current is completely transferred to switch  $S_1$  due to snubber inductor  $L_{S1}$ . As the result, switch  $S_1$  is turned on with the ZCS condition, and the circuit operation Modes 1–6 repeat.

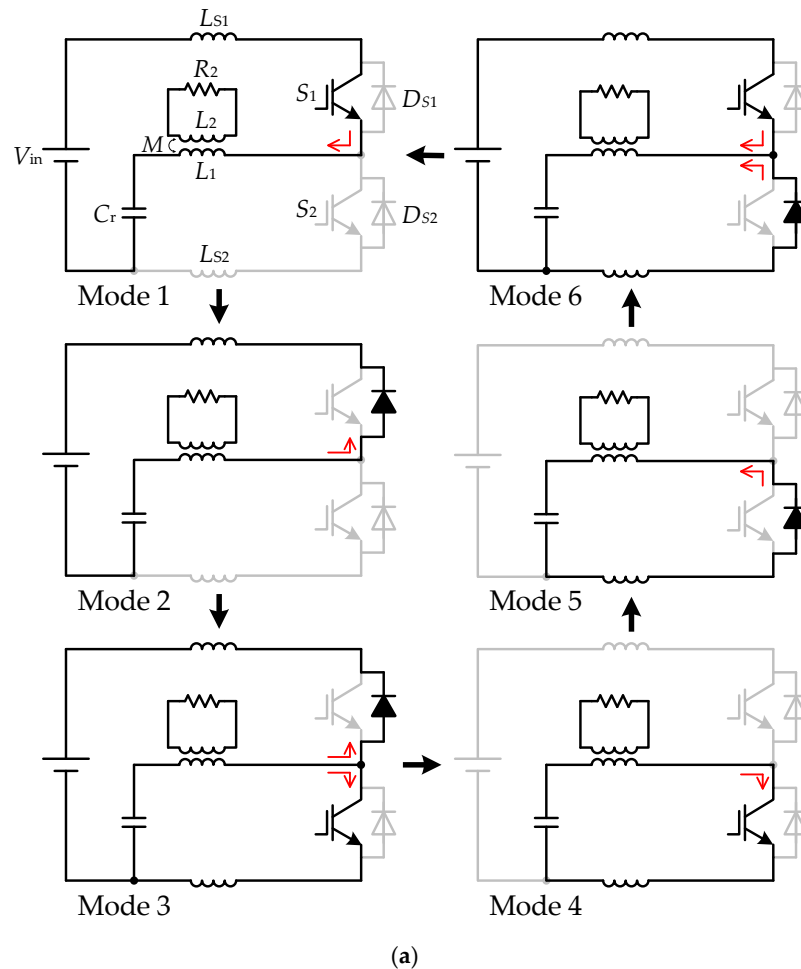


Figure 5. Cont.



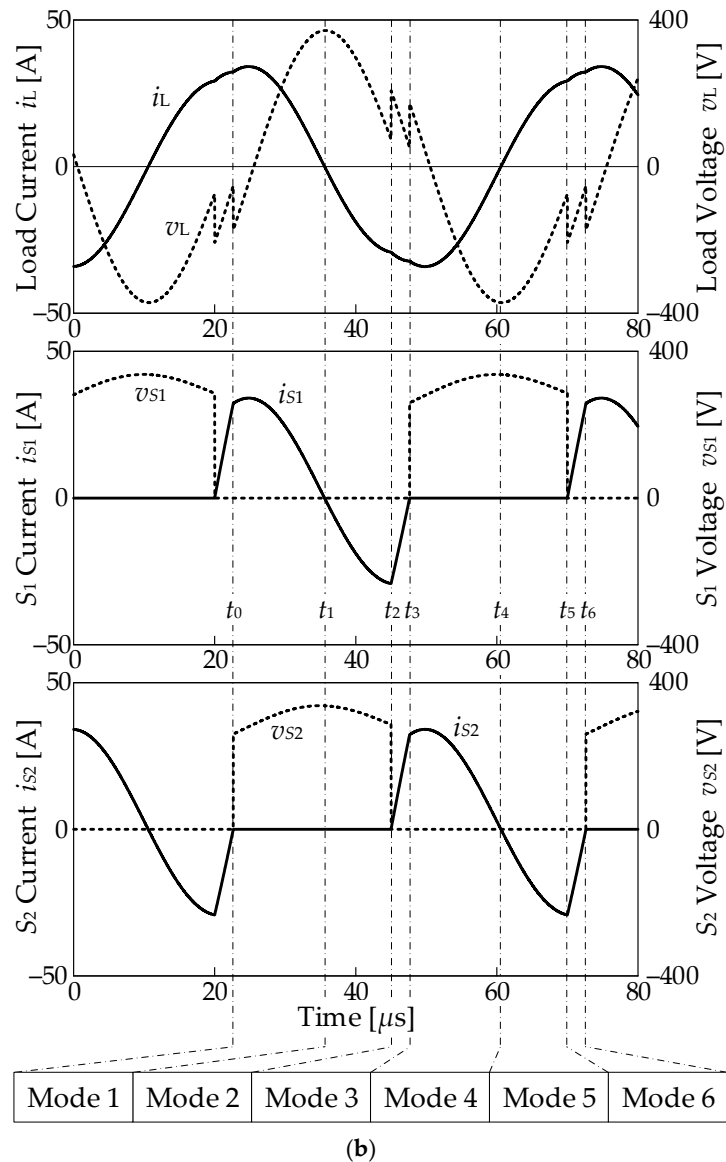


Figure 5. Operating conditions. (a) Circuit mode transitions. (b) Operating waveforms by simulations.

#### 4. Experimental Results and Performance Evaluations

##### 4.1. Voltage and Current Waveforms

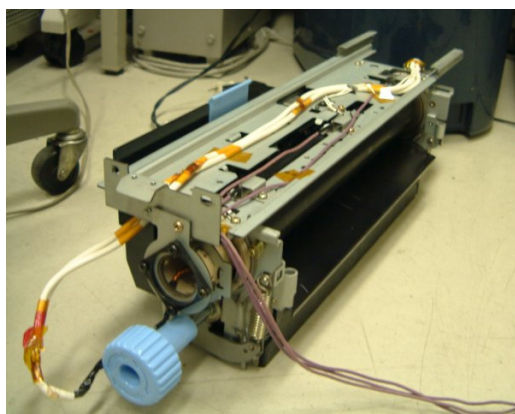
The parameters and specifications of the circuit design for the high-frequency PDM-controlled soft-switching series load resonant inverter are listed in Table 1. Inductors  $L_{S1}$  and  $L_{S2}$  are set to  $12 \mu\text{H}$ , as determined by the IGBT's peak voltage of 350 V. For this circuit, the  $di/dt_{\text{max}}$  stress is  $12.5 \text{ A}/\mu\text{s}$  dynamic switch current and  $3.8 \mu\text{s}$  current overlapping time. Figure 6 shows the IH fixed roller and installed heating coil self-inductance  $L_1$ . The heating coil, shown in Figure 6b, has a diameter of 50 mm and a width of 350 mm.

The operating waveforms of voltage  $v_L$  and load current  $i_L$  for PDM duty ratios  $D_{\text{PDM}} = 0.8$  and  $0.2$  are given in Figure 7. They show that the proposed high-frequency inverter can operate with PDM control.



**Table 1.** Circuit design specifications.

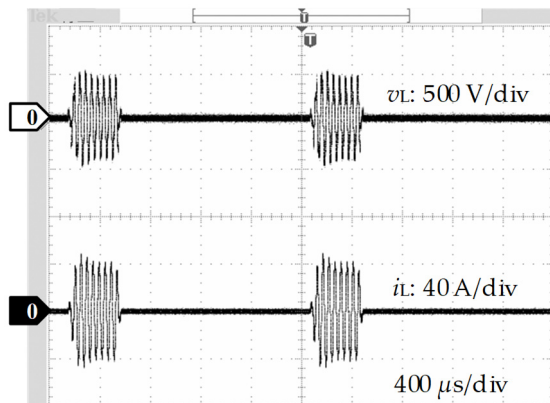
Item	Symbol	Value
DC input voltage	$V_{in}$	280 V
Resonant capacitor	$C_r$	0.49 $\mu\text{F}$
Frequency of switching	$f$	20 kHz
Frequency of PDM	$f_{PDM}$	400 Hz
Snubber inductor	$L_{S1}, L_{S2}$	12 $\mu\text{H}$
Heating coil self-inductance	$L_1$	90 $\mu\text{H}$
IH load time constant	$\tau$	9.23 $\mu\text{s}$
Electromagnetic coefficient of coupling	$k$	0.48
IGBT (Mitsubishi: CT75AM-12)	$I_C$	75 A
	$V_{CE}$	600 V



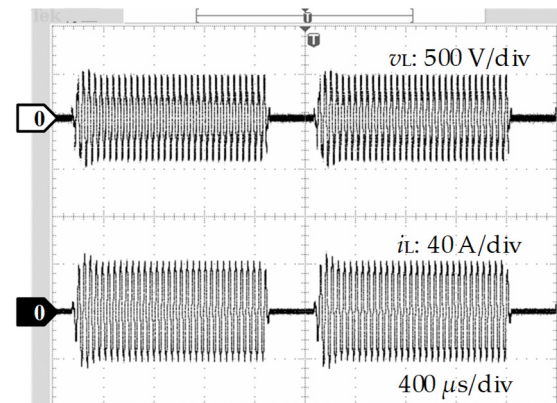
(a)



(b)

**Figure 6.** IH fixed roller and heating coil. (a) Fixed roller. (b) Heating coil.

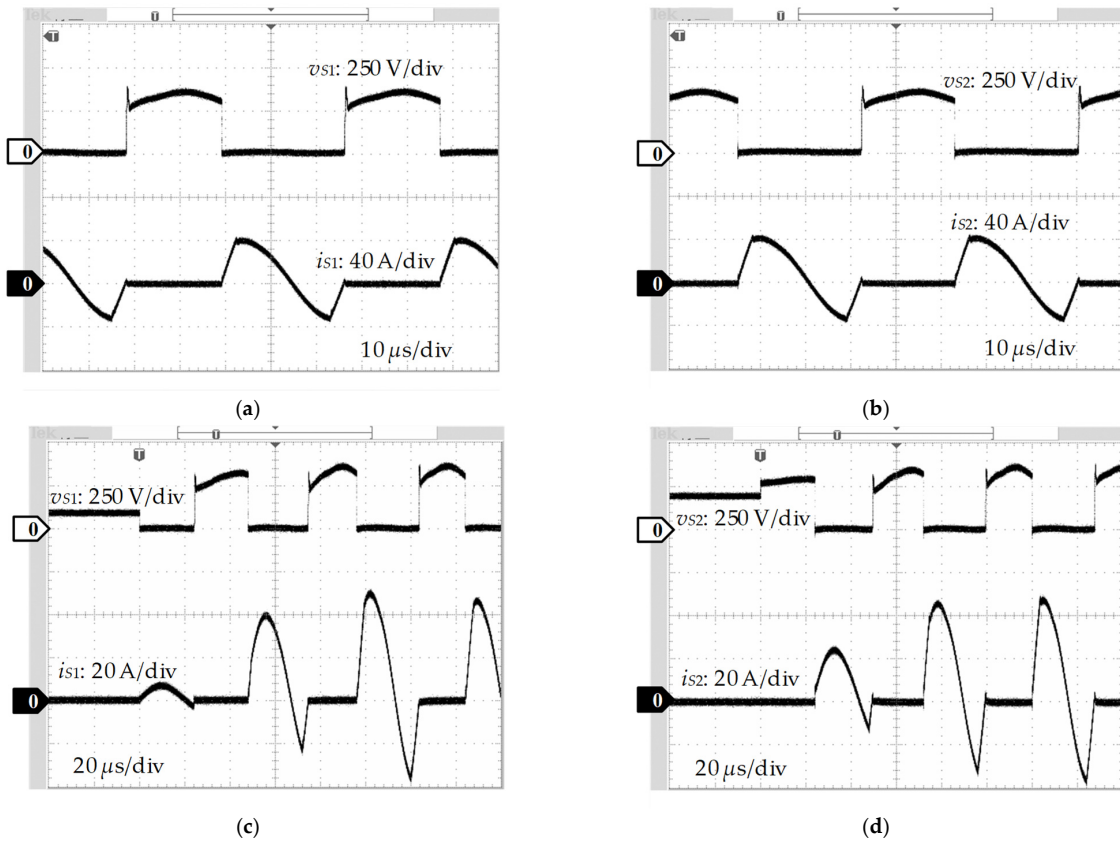
(a)



(b)

**Figure 7.** Load current  $i_L$  and voltage  $v_L$  waveforms under PDM. (a) Duty ratio  $D_{PDM} = 0.2$ . (b) Duty ratio  $D_{PDM} = 0.8$ .

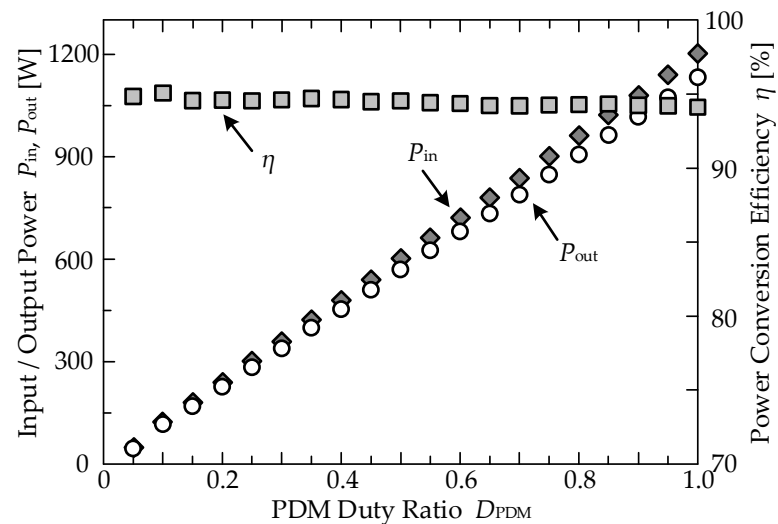
Figure 8a,b illustrate the operating waveforms of the current and voltage of the power semiconductor switches  $S_1$  and  $S_2$ . These figures show that ZCS soft-switching commutation is achieved in the transitions from turn-on and turn-off. The waveforms of the current and voltage of switches  $S_1$  and  $S_2$  are shown in Figure 8c,d for the beginning interval of the injection of power. Observing waveforms in Figure 8c,d, the switches  $S_1$  and  $S_2$  also operate for PDM control implementation using complete ZCS soft-switching commutation.



**Figure 8.** Current and voltage waveforms for switches  $S_1$  and  $S_2$ . (a) Steady-state condition for switch  $S_1$ . (b) Steady-state condition for switch  $S_2$ . (c) Beginning of power injection for switch  $S_1$ . (d) Beginning of power injection for switch  $S_2$ .

#### 4.2. Power Conversion Efficiencies

The power conversion efficiencies and input/output for the soft-switching high-frequency inverter are given in Figure 9. Changing the PDM duty ratio  $D_{PDM}$  causes linear regulation of the output. The PDM operates at  $D_{PDM} = 1.0$  in the printing mode and at  $D_{PDM} = 0.05$  in the stand-by mode. More than 94% power conversion efficiency  $\eta$  can be achieved with a  $D_{PDM} = 0.05$  to 1.0. Thus, the proposed IH fixed roller application in printing and copy machines can achieve high efficiency using the proposed high-frequency inverter system.



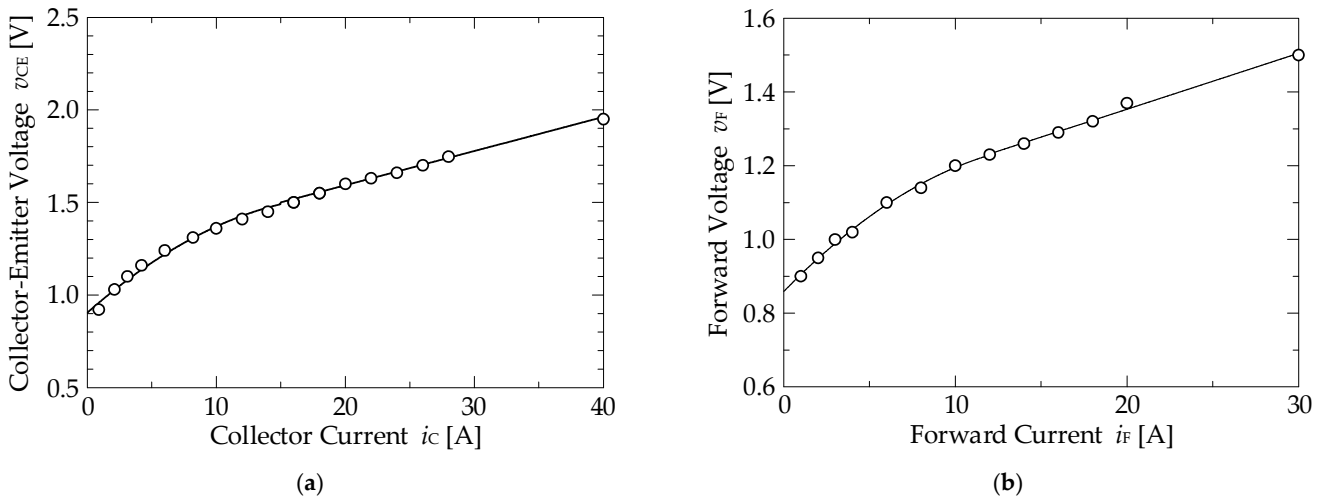
**Figure 9.** Power conversion efficiency and input/output characteristics.

### 4.3. Analysis of Power Loss

The high-frequency soft-switching power losses of the proposed inverter are extremely low. IGBT fall current and tail current losses are almost zero due to ZCS commutation. Additionally,  $L_1$  and snubber inductors  $L_{S1}$  and  $L_{S2}$  conduction losses are negligible due to litz wire usage. The IGBT conduction losses of the proposed high-frequency inverter are the main power losses. The IGBT voltage and current characteristics curves are used for conduction power losses calculations. Figure 10 shows the current and voltage characteristics of the IGBT and that its antiparallel diode has constant temperature conditions. Experimental results yielded the switching characteristics curves. Equations (13) and (14) represent the characteristic curves, which approximate quadratic polynomials in the low forward current area and linear functions in the high forward current area.

$$\begin{cases} v_{CE} = -0.0015 i_C^2 + 0.0616 i_C + 0.904 & (i_C < 15A) \\ v_{CE} = 0.0185 i_C + 1.223 & (i_C \geq 15A) \end{cases} \quad (13)$$

$$\begin{cases} v_F = -0.00141 i_F^2 + 0.0477 i_F + 0.859 & (i_F < 12A) \\ v_F = 0.0152 i_F + 1.05 & (i_F \geq 12A) \end{cases} \quad (14)$$



**Figure 10.** Current and voltage characteristics of IGBT and diode. (a) IGBT for  $S_1$  and  $S_2$ . (b) Diode for  $D_{S1}$  and  $D_{S2}$ .

The conduction power loss calculations of the semiconductor are introduced into the simulation algorithm by these equations. Using the above equations in a circuit simulation, the conduction power losses of the diodes and IGBTs can be calculated. Additionally, using Equation (15) and the experimental results, other stray power losses of the reverse recovery losses of the diodes and switching power losses of the IGBT can be estimated separately from the inverter total power losses [29,30]. The power losses analysis results are given in Figure 11.

$$(\text{Total power losses}) - (\text{Conduction power loss}) = (\text{Other stray power loss}) \quad (15)$$

In this result, it is obvious that the  $D_{PDM}$  ratio of this PDM control scheme increases proportionately with the power losses increase. When the printing mode  $D_{PDM}$  ratio reaches 1.0 (heaviest load), only 20% of the total power losses are stray power losses and 80% are conduction power losses. This results from the ZCS soft commutation display low power losses, as seen in Figure 11.

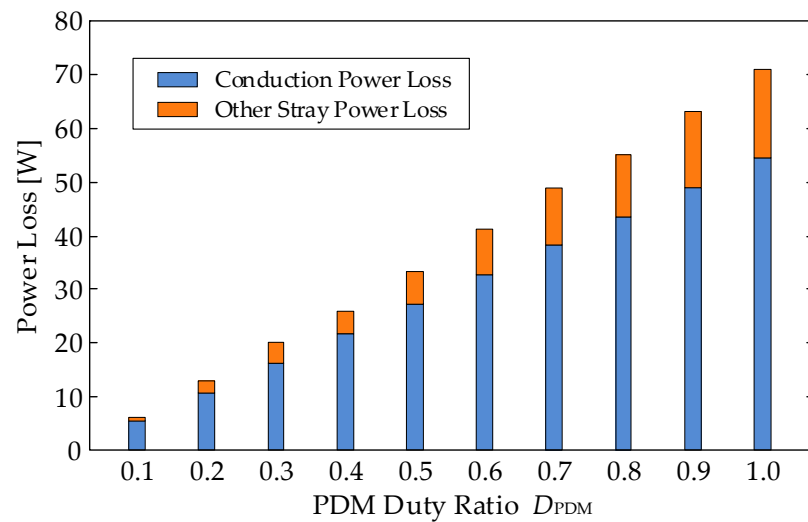


Figure 11. Proposed high-frequency inverter power losses analysis.

#### 4.4. Halogen Lamp Heater Comparative Characteristics

A comparison of the temperature rise characteristics of the halogen lamp and IH fixed roller heater is given in Figure 12. The graph clearly shows that the IH fixed roller temperature rise is significantly faster than that of the halogen lamp heater.

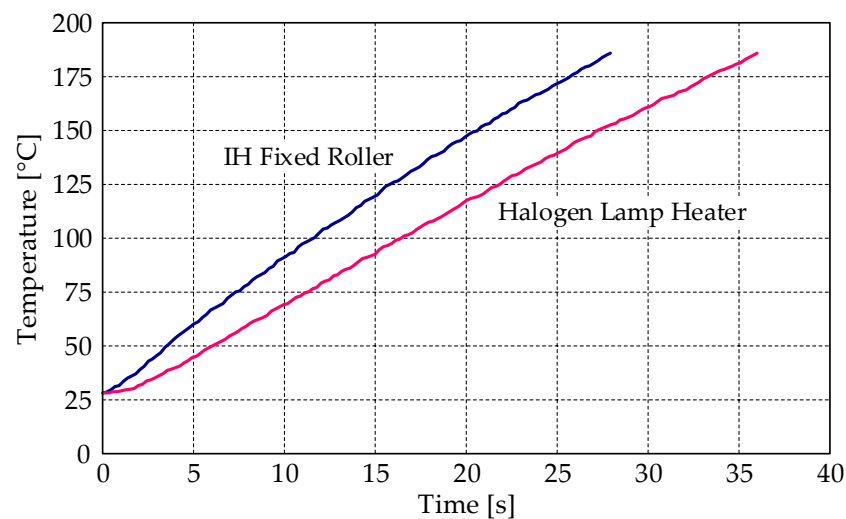


Figure 12. Temperature rise characteristics.

At an output power of 1200 W, the rise time to reach 185 °C is shown in Table 2. The table compares the rise time and the power consumption of a halogen lamp and an IH fixed roller heater. The Table 2 shows the lower rise time of 27.9 s for the IH fixed roller, while it is 36.1 s for the halogen lamp heater. Additionally, the IH fixed roller uses only 52 Wh, whereas the halogen lamp heater uses 57 Wh in the 100 °C idling mode. Therefore, there is a 9% improvement in the energy consumption.

Table 2. Characteristics.

Item	IH Fixed Roller	Halogen Lamp Heater
Rise time to 185 °C	27.9 s	36.1 s
Idling mode power consumption	52 Wh	57 Wh

## 5. Conclusions

This paper has presented an IH fixed roller high-frequency PDM-controlled series load resonant soft-switching inverter application which is used in printing and copy machines. The operation of the steady-state PDM-controlled inverter's experimental results are analyzed and evaluated. The proposed high-frequency resonant inverter is operated under the principle of zero-current soft switching across a wide power regulation range by using the PDM control scheme. When the printer uses the output power at very light load conditions such as the stand-by mode, the PDM duty ratio  $D_{PDM}$  is at a very small value, which is 0.05 in this experiment. This small output power requires only two or three cycles of injected current from the voltage power source. Therefore, the asymmetrical pattern of PDM pulses is employed so that the injected current becomes easily observable and the control circuit has enough time to get the heat response from the IH system. Then, the ZCS operations are verified at very light load conditions. The power conversion efficiency for power output ranges from 50 to 1200 W is achieved at  $\eta > 94\%$ . Power loss calculations are verified through experimental  $i-v$  characteristics of the diode and IGBT. At heavy load conditions, the stray load power losses amount to be only 20% of the total power losses. This is due to the soft commutation of the ZCS, which yields very low switching power losses. At light load conditions, although the power conversion becomes less effective, the ZCS operations are still achieved. Additionally, the power losses saved by the operations are significant due to the fact that most of the printer operation time is in the stand-by mode. Importantly, the experimental results demonstrate good performance of the proposed high-frequency resonant inverter by replacing the conventional halogen lamp heater with the IH fixed roller. Therefore, the PDM-controlled series load resonant soft-switching high-frequency inverter is proved to be effective for IH applications. Future evaluations of this proposed high-frequency inverter are planned using new wide-bandgap semiconductors, such as GaN FET.

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